I will discuss some recent progress in using lattice QCD to perform first-principles calculations of the spectra of mesons. In particular, I will highlight some new results on resonances, near-threshold states and related scattering phenomena -- this is a theoretically and experimentally interesting area where we have made significant advances in the last few years.